

**EXAM II, MTH 211, Fall 2009**

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**QUESTION 1.** We want to tile a plane using one type of triangles, say  $ABC$ , Color the angle  $A$  with red, color the angle  $B$  with green, and color the angle  $C$  with blue. We want to do the tiling so that all around  $A$  is red, all around  $B$  is green, and all around  $C$  is blue. What type of triangles must we use? How many triangles of this type are there? GIVE a MATHEMATICAL justification for your answer.

**QUESTION 2.** Let  $C$  be a circle of radius 2 cm with CENTER  $O$ , and  $ABC$  is a triangle such that  $|OA| = |OB| = 4$ , and  $|OC| = 8$ . Sketch the inversion of the triangle  $ABC$  with respect to the circle  $C$ . what is the Euclidean distance between  $Inv(A)$  and  $Inv(C)$ .

**QUESTION 3.** Let  $ABC$  be a triangle with vertices  $(2, 0)$ ,  $(2, 1)$ , and  $(3, 1)$ . Rotate  $ABC$  around the origin 60 degrees. Then we get a new triangle  $A'B'C'$ . Find the vertices  $A'$ ,  $B'$ , and  $C'$ . (note  $\cos(60) = 1/2$ ,  $\sin(60) = \sqrt{3}/2$ .)

**QUESTION 4.** Let  $H$  be a hyperbolic circle with center  $O$  and radius 2cm. Locate two points inside  $H$ , say  $A$  and  $B$ , such that  $C_A$  is parallel to  $C_B$ , then connect  $A$  to  $B$  by a hyperbolic line.

**QUESTION 5.** Let  $H$  be a hyperbolic circle with radius 2 and center  $O$ . Construct inside  $H$  a hyperbolic circle with a hyperbolic radius equals to  $\ln(3)$ .

**QUESTION 6.** Let  $H$  be a hyperbolic circle with radius 2. Let  $B$  be a point on  $H$  (so  $B$  is a horizon point). Construct two parallel hyperbolic lines, say  $L_1$  and  $L_2$ , such that  $L_1$  meets  $L_2$  at  $B$ . (another way of saying that: using EUCLIDEAN eyes , parallel hyperbolic lines might interest!!!). State briefly the steps of construction.

**QUESTION 7.** What type of of Freize pattern is the below? Given that we initially started with the letter b.

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